



# Flowering in bursting bubbles with viscoelastic interfaces

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**The lifetime of bubbles, from formation to rupture, attracts attention because bubbles are often present in natural and industrial processes, and their geometry, drainage, coarsening, and rupture strongly affect those operations. Bubble rupture happens rapidly, and it may generate a cascade of small droplets or bubbles. Once a hole is nucleated within a bubble, it opens up with a variety of shapes and velocities depending on the liquid properties. A range of bubble rupture modes are reported in literature in which the reduction of a surface energy drives the rupture against inertial and viscous forces. The role of surface viscoelasticity of the liquid film in this colorful scenario is, however, still unknown. We found that the presence of interfacial viscoelasticity has a profound effect in the bubble bursting dynamics. Indeed, we observed different bubble bursting mechanisms upon the transition from viscous-controlled to surface viscoelasticity-controlled rupture. When this transition occurs, a bursting bubble resembling the blooming of a flower is observed. A simple modeling argument is proposed, leading to the prediction of the characteristic length scales and the number and shape of the bubble flower petals, thus paving the way for the control of liquid formulations with surface viscoelasticity as a key ingredient. These findings can have important implications in the study of bubble dynamics, with consequences for the numerous processes involving bubble rupture. Bubble flowering can indeed impact phenomena such as the spreading of nutrients in nature or the life of cells in bioreactors.**

bubble | surface | protein | flowering

When residing in Newtonian fluids, bubble rupture proceeds with features that are shown in Fig. 1. Different dynamics are observed depending on the capillary number,  $Ca = u \eta / \gamma$ , where  $u$  is the experimentally measured characteristic retraction speed of the film,  $\eta$  is the liquid viscosity, and  $\gamma$  is the surface tension between the liquid and gas, and the Reynolds number,  $Re = \rho u R_{\text{bubble}} / \eta$ , where  $\rho$  is the liquid density, and  $R_{\text{bubble}}$  is the bubble radius (1–7). Fig. 1 *A–D* report observed bubble ruptures in the different regimes previously discussed in the literature: 1) for  $Re \ll 1$ , viscous forces are larger than inertial and surface forces, resulting in a very slow hole opening (8) (Fig. 1*A*); 2) when  $Re > 1$ , the hole opens up much more quickly (9), and a toroidal rim (Fig. 1*B*) is subjected to an azimuthal instability, which leads to fingering and, possibly, jetting (Fig. 1 *B–D*), depending on the corresponding  $Ca$  value. If  $Ca \gg 1$ , the rim is stable and folds upward (10); otherwise, inertial instabilities break it into pieces with a characteristic length scale,  $d = \sqrt{R_{\text{bubble}} h}$ , where  $h$  is the film thickness (11).

Here, we report evidence of the effect of surface viscoelasticity in bubble rupture dynamics. Surface viscoelasticity is adjusted by adding a surface-active material to the bulk and modulating its concentration and chemistry. We chose bovine serum albumin (BSA) proteins (12, 13), as they are known to form highly viscoelastic surface layers. At low concentrations, BSA molecules are adsorbed at the air/water interface with their major axis parallel to the surface. No protein denaturation occurs, and the

molecules retain their globular conformation. As the concentration of BSA increases, a primary monolayer achieves full surface coverage, and a secondary monolayer appears, extending into the aqueous phase (14, 15). Adsorbed protein molecules are connected by interprotein contacts forming an interconnected network within the adsorbed layers (16). Upon compression, globular proteins, such as BSA, respond as deformable spheres, thereby being capable of storing elastic energy (yielding high storage moduli) (17). Many examples can be found in the literature in which the addition of surfactants to the protein solution can drastically change surface properties, giving an unlimited variety of model systems to achieve desired surface properties with a straightforward tuning of the surfactant concentration (18).

## Results and Discussion

Surface elasticity introduces another dimensionless parameter, the elastocapillary number (19),  $E_c = \frac{E_d}{\gamma}$ , where  $E_d$  is the surface initial dilatation modulus measured for each concentration (*SI Appendix*). We carried out an extensive array of experiments to analyze the effects of  $E_c$  on the bubble rupture dynamics.

We report that surface viscoelasticity drives bubble rupture during opening, and the rupture shape changes as the concentration of BSA

### Significance

The bursting bubbles are central in many natural and engineering processes because they influence the heat, mass, and momentum transfer; for example, fragmentation and cell death are influenced by the mechanical stresses produced by the hydrodynamic flows caused by the fast and frequent bubble bursting on viscoelastic surfaces in bioreactors. We investigate the bursting bubbles with viscoelastic interfaces and demonstrate that the interfacial viscoelasticity changes the bubble rupture mode. We present the characteristics of the bubble rupture mode that produces flower-shape bubble bursting and a validated modeling that can predict the number of petals formed during the rupture. This work presents insights for understanding and controlling the bursting bubbles with viscoelastic interfaces with both fundamental and practical implications.

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The authors declare no competing interest.

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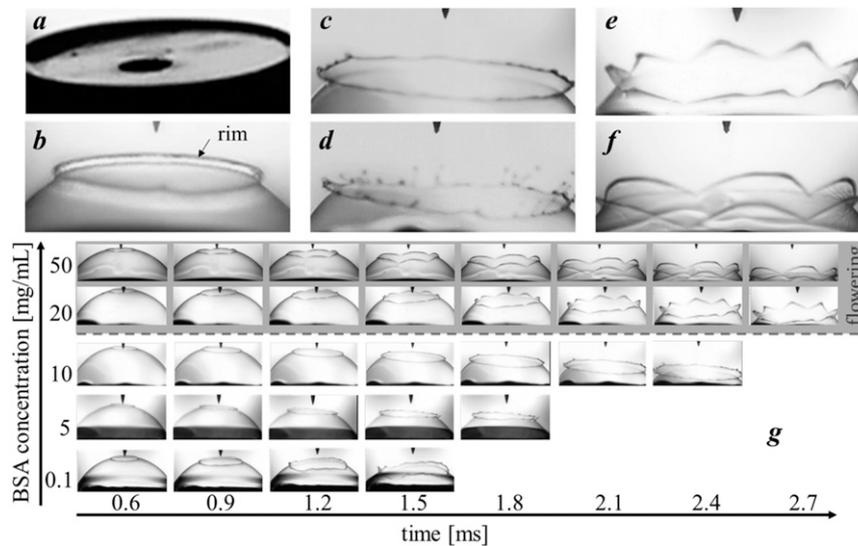
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**Fig. 1.** Bubble bursting dynamics. (A) Low  $Re$ . (B and C) High  $Ca$  and high  $Re$ . (D) Low  $Ca$  and high  $Re$ . (E) Low  $Ca$  and high  $Re$  with intermediate interfacial viscoelasticity (20 mg/mL of BSA). (F) Low  $Ca$  and high  $Re$  with high interfacial viscoelasticity (50 mg/mL of BSA). (G) Bubble rupture as functions of time for different concentrations of BSA. Increasing the concentration of BSA leads to an increase in the surface viscoelasticity, and the bubble bursting dynamics change. The concentration of 20 mg/mL is identified as the limit above which flowering occurs. The number of petals, 10 at 20 mg/mL, decreases to 5 when the concentration of BSA is increased to 50 mg/mL. The bursting time (from the puncture to complete film retraction) increases when BSA is added, and it changes from 1.5 ms at 0.1 mg/mL to 2.7 ms at 50 mg/mL.

increases (Fig. 1 E and F) (Movie S1). In later stages of bubble rupture at a high BSA concentration in Fig. 1G (20 mg/mL shown in Movie S2, 50 mg/mL shown in Movie S3, and 15 mg/mL shown in Movie S4), we observe that the rim fractures during opening, thus forming liquid petals similar to a flower blooming.

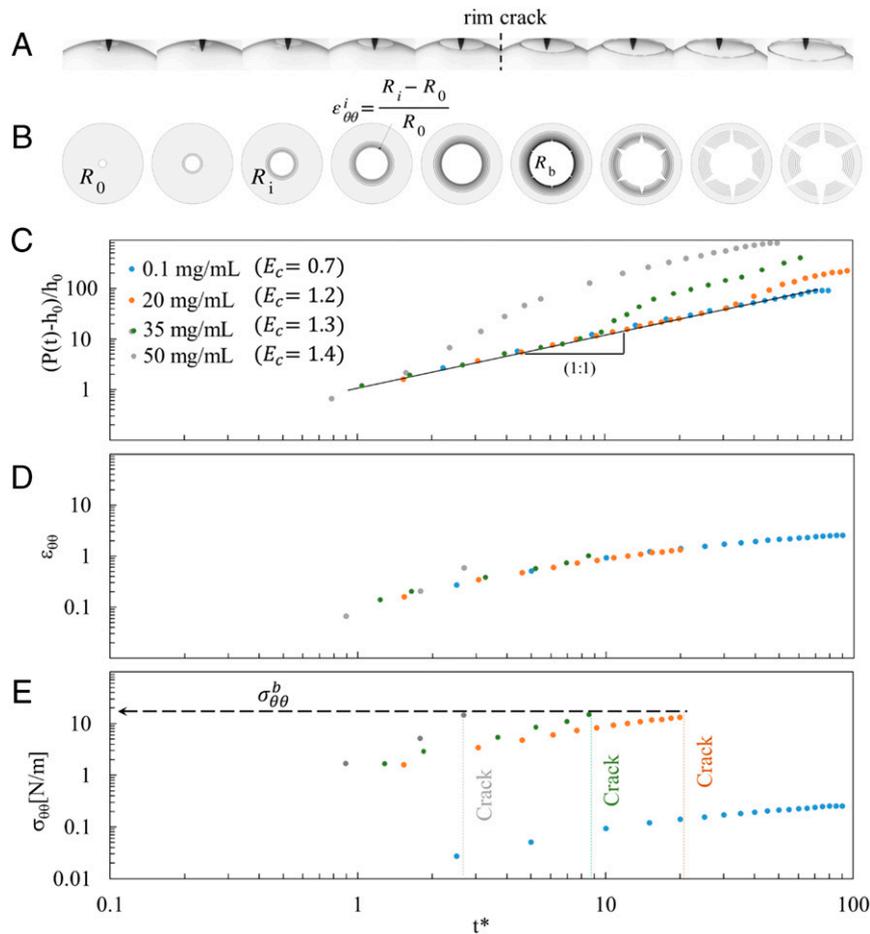
The complete picture observed in the experiments at large BSA concentrations is shown in Fig. 2B: the initial stage of hole opening (with the radius equal to  $R_0$ ) sees the formation of a toroidal rim (with the radius equal to  $R_i$ ) that progressively grows in diameter followed by a developing rim breaking into small pieces (when the radius reaches  $R_b$ ). The final stage has cracks growing radially through the bubble film with a velocity higher than the rim retraction speed producing triangular- or trapezoidal-shaped strips. The combined effects of inertia and capillarity lead to an outward trajectory of the strips and formation of a flower-shape rupture. A schematic of the experimental observation is reported in Fig. 2A.

We quantitatively illustrate the opening dynamics by following the hole perimeter rather than its radius since the perimeter ( $P$ ) also accounts for the borders created by the cracks. At the lowest concentration in which interfacial viscoelasticity is less important, the trend shown in Fig. 2C is very similar to that found by Petit et al. and McEntee et al. (10, 20) for bubbles lacking viscoelasticity with an initial long linear increase of the rim perimeter, corresponding to a constant opening velocity. The behavior is similar to the inertial regime predicted by Culick and Taylor (9) but with a slower velocity, and Petit et al. (20) ascribe such a slowing down to the surface properties in the presence of surfactants. We reported the retraction speed of the rim,  $u$ , before the rim crack, as a function of the BSA concentrations in Fig. 3C, where  $u_c$  is the Taylor–Culick velocity,  $u_c = \sqrt{\frac{\phi}{\rho} \frac{\gamma}{h}}$ , [ $\gamma$  is the surface tension, and  $\phi$  is a constant ca. 2 depending on the film thickness (10)]. The decrease of velocity is ca. 20% at the highest concentration of BSA, and it affects  $Re$  ( $\sim 10^3$ ) and  $Ca$  ( $\sim 1$ ); however, no different bursting dynamics are expected from the literature (3). However, at larger surface concentrations (20, 35, and 50 mg/mL), the rim opening follows three sequential regimes: an initial regime with the rim opening following a

constant velocity similar to that at lower concentrations, a faster intermediate regime that commences following rim cracking ( $t = t_{\text{crack}}$ ) and petal blooming, and a final regime, which is initiated when crack propagation stops corresponding to a slowdown of the rim opening. In a dimensionless form, the data (Fig. 2C) for the three different BSA concentrations superimpose in the initial regime, thus confirming the time scaling ( $t^* = \frac{t}{\tau}$ ). Also notice

that in the intermediate faster regime, the cracks propagate within the viscoelastic membrane at a velocity comparable with the sound velocity (refer to the data in SI Appendix) as found by Huang et al. (21). The cracks propagate into the membrane, releasing elastic energy stored during the bubble inflation process and stop once the elastic energy is consumed, thus attaining the final regime in Fig. 2C.

**Modeling.** The expansion of the rupture opening produces a strain in the membrane defined by a strain tensor,  $\varepsilon$ , which is discussed in greater detail in SI Appendix. The hoop deformation of the rim ( $\varepsilon_{\theta\theta}$ ) up to the inception of cracking (Fig. 2D) is used to estimate the hoop surface stress as  $\sigma_{\theta\theta} = E_s \varepsilon_{\theta\theta}$ , with  $E_s$  as the surface dilatational elastic modulus (SI Appendix), shown in Fig. 2E. The result does not change if one considers the expected change in the surface elastic modulus due to the change in BSA concentration during the rim retraction. For larger surface concentrations (20, 35, and 50 mg/mL), stress data are reported up to the appearance of cracks since, when cracks develop, the actual stress cannot be easily estimated. It is apparent that at larger BSA concentrations, the stress level attained at the onset of cracks does not depend on BSA concentration,  $\sigma_{\theta\theta}^b$  in Fig. 2E, while for  $c_{\text{BSA}} < 20$  mg/mL, that is, when cracks do not form, such a critical stress is not attained. In passing, it is worth remarking that the critical hoop surface stress is comparable with the surface elastic dilatational modulus in agreement with results of Tabuteau et al. (22) for brittle fractures in viscoelastic fluids. We identify the conditions for the bubble flowering in the value of  $E_c$ ; when it is bigger than one, the initial dilatational modulus is sufficiently high to induce fragile cracks on the opening rim,

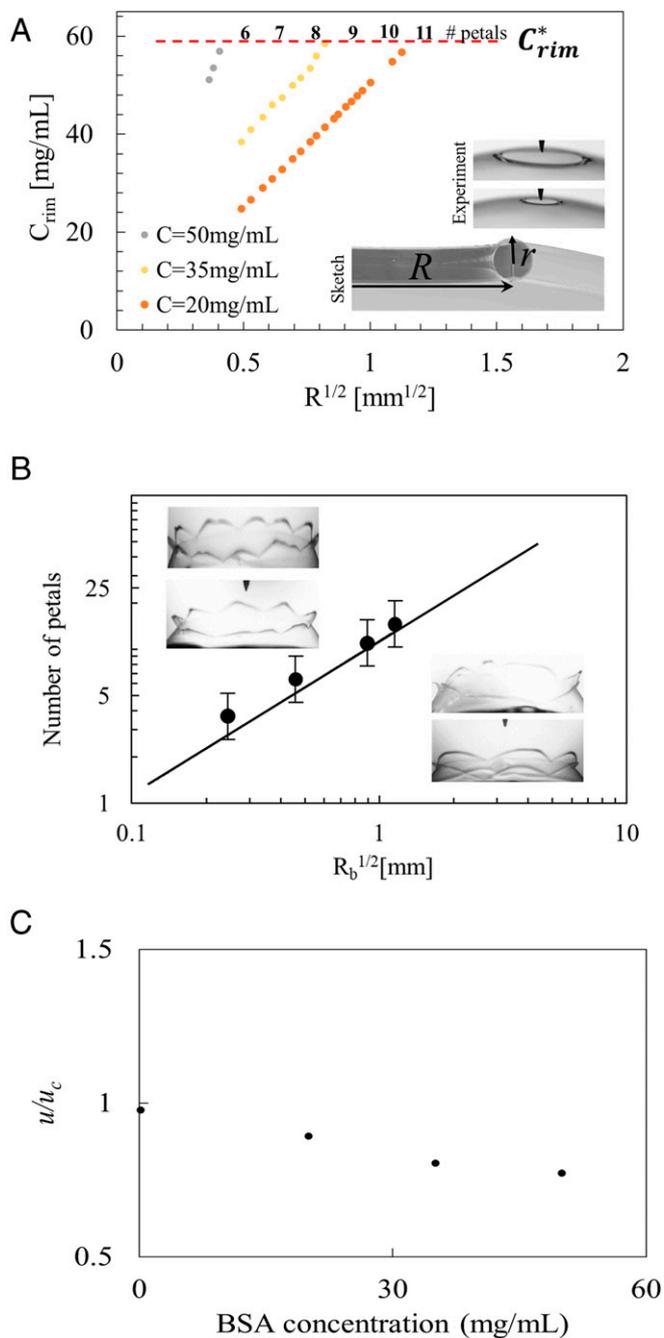


**Fig. 2.** Two-step mechanism to form bubble flowering. (A) Experimental evidences of two rupture regimes for BSA concentration equal to 20 mg/mL. (B) Rim deformation ( $\epsilon_{\theta\theta}^i$ ) sketched in the two rupture regimes, where  $R_i$  is the rim radius at time  $i$  and  $R_0$  is the initial rim radius. (C) Dimensionless perimeter as function of dimensionless time ( $t^* = \frac{t}{P_0}$ ), where  $t$  is the experimental time and  $P_0$  is the perimeter of the first observed hole. (D) Hoop strain as function of dimensionless time, calculated as shown in *SI Appendix*. (E) Hoop surface stress ( $\sigma_{\theta\theta}$ ) as function of dimensionless time is calculated as  $\sigma_{\theta\theta} = E_c \epsilon_{\theta\theta}$ .

while when it is less than one, the surface tension drives the bursting phenomenon.

Analyzing the crack formation and the successive bubble flowering, it is useful to compare the observations presented here with what has been established for filaments of viscoelastic liquids that break with brittle cracks in uniaxial extensional flows at sufficiently high Weissenberg numbers, defined as  $Wi = \dot{\epsilon}_{\theta\theta} \lambda$ , where  $\dot{\epsilon}_{\theta\theta}$  is the hoop strain rate and  $\lambda$  is the surface relaxation time as calculated in *SI Appendix* (21). The number of cracks is also found to be proportional to the diameter of the filament at the crack formation (23). The present experiments represent biaxial stretching of viscoelastic films and complement the stretching of viscoelastic filaments but with important distinctions. In the experiments reported here, the hole opening the rim is subjected to an extensional flow that is modeled as a uniaxial stretching with strain rate given by  $\dot{\epsilon}_{\theta\theta}$  measured at the rim border ( $\dot{\epsilon}_{\theta\theta} = \frac{\dot{R}}{R}$ ), and the formation of multiple cracks determines the number of observed petals in the flowering. We here propose a simple argument to predict the number of petals in bubble flowering based on three assumptions: 1) all the fluid of the disappearing film collects into the rim, and 2) film drainage is negligible (24, 25), and 3) the BSA accumulates on the rim from the disappeared film. The actual volume of the rim is  $V_R = 2\pi^2 r^2 R$ , with  $R(t)$  the actual major radius and  $r(t)$  the minor

radius of the toroidal uncracked rim (Fig. 3A), which here plays the role of the filament. The volume of the material subtracted from the bubble by the advancing rim is  $V_S = \pi R^2 h$ . Mass conservation implies  $V_R = V_S$ , and, assuming no drainage during the bubble inflation (as verified by interferometric measurements in *SI Appendix*) and that the assumption that the number of cracks is proportional to the filament diameter (23), the number of petals scales as  $R_b^{1/2}$  (Fig. 3B). The experimental results, in terms of hole radius at crack inception and the number of observed cracks, support this scaling as shown in Fig. 3A. Furthermore, the experiments show that the rim breaks when the local BSA concentration in the rim reaches the same value (of that corresponding to the critical stress defined above). Hence, data from one experiment can be used to determine this critical concentration,  $C_{rim}^*$ , and for calculating the number of petals formed during bubble flowering (Fig. 3A) in subsequent experiments. The critical concentration is well defined by the propagation of independent, simultaneous, multiple cracks that resemble a brittle fracture. Usually, in solids, a brittle fracture starts from microimperfections in the material; in our viscoelastic thin rim, the brittle fracture, which arises due to the high  $E_c$  and deformation rate, may also start from microimperfections, which are not able to heal sufficiently fast. Qualitatively, we can speculate that the



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